

# Wiring American Flyer Sectional Track

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Version 1.0 of April 2020



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# 1. Introduction

There are many options for routing wire between a transformer and American Flyer sectional track. This document evaluates the impact of wire gauge (AWG) number of connections, and routing of wires to a notional loop consisting of 40 sections of American Flyer sectional track: 12 curve and 28 straight. Seven different cases are examined for six different gauges of wire and 3 different values of track resistance.

In comparing the options, the following metrics were considered:

1. The difference between the highest and lowest resistance of points on the track as measured from the transformer terminal. This difference reflects the variability in speed the engine will experience as it completes a revolution of the track. Experiments conducted on my layout (using a 12B transformer) indicate a difference of 0.5 ohms is barely noticeable at low speeds, but not at high speeds. Allocating half of this resistance difference to each of the two conductors / rails, desirable performance is for each conductor / rail to have a resistance difference of no more than 0.25 ohms. Marginal performance is attributed to a resistance difference of between 0.25 ohms and 0.5 ohms. Undesirable performance is attributed to a resistance difference greater than 0.5 ohms.
2. The average resistance from the sample points to the transformer terminal is not an issue unless it becomes so large that the train engine cannot achieve a reasonable speed when the transformer is at its maximum setting. Subjectively, I determined that the average resistance for each conductor / rail would have to exceed about 0.75 ohms with my 12B transformer before becoming excessive. This only occurs for Case 1, hence average resistance was not used as a discriminator.
3. While cost is always of concern, none of the cases used more than 100 ft, and the cost difference between 100 feet of the smallest (22 AWG) and largest (12 AWG) wire is only on the order of \$8 if speaker wire is used. See Table 1 for details.

Table 1: Cost of Cable (as of March 29, 2020)

| AWG    | length | single conductor stranded | Source | Speaker Wire | Source             | ROMEX house wiring | Source     |
|--------|--------|---------------------------|--------|--------------|--------------------|--------------------|------------|
| 22 AWG | 100 ft | \$9.95                    | Jameco | \$10.95      | Audiopipe - Amazon |                    |            |
| 20 AWG | 100 ft | \$12.95                   | Jameco | \$11.95      | Audiopipe - Amazon |                    |            |
| 18 AWG | 100 ft | \$18.95                   | Jameco | \$12.95      | Audiopipe - Amazon |                    |            |
| 16AWG  | 100 ft | \$20.95                   | Jameco | \$14.95      | Audiopipe - Amazon |                    |            |
| 14AWG  | 100 ft |                           |        | \$16.89      | Audiopipe - Amazon | \$31.57            | Home Depot |
| 12AWG  | 100 ft |                           |        | \$18.95      | Audiopipe - Amazon | \$48.57            | Home Depot |

Three different values of track resistance are used because one of the critical factors for track resistance is the degree that the track connectors make good electrical contact. I connected together ten pieces of American Flyer section track without making any special effort to establish a good electrical connection. The resistance of one rail was 0.75 ohms while the other was 1.61 ohms. Based on these measurements, I selected three values of track resistance per section to use in this analysis: 0.025 ohms, 0.075 ohms, and 0.15 ohms. The lower value (0.025 ohms) reflects a value that should be attainable with careful attention to establishing a good electrical connection. The middle value (0.075 ohms) reflects a value attainable with a reasonable effort to establish a good electrical connection, or that value that may happen as the electrical conductivity degrades over time. The higher value (0.15 ohms) reflects a value where little attention has been paid to establishing good electrical conductivity, or where the electrical conductivity has degraded over time.

A desirable configuration achieves the desirable resistance difference for the middle value of track resistance. A highly desirable configuration achieves the desirable resistance difference for the higher value of track resistance.

The resistance per foot of copper wire is listed in Table 2. The source for this data is ASTM B8 and is applicable for 20° C (68° F) which is a reasonable room temperature for a train layout.

*Table 2: Resistance (ohms) per foot of stranded copper wire*

|         |         |        |         |        |        |
|---------|---------|--------|---------|--------|--------|
| 12 AWG  | 14 AWG  | 16AWG  | 18AWG   | 20AWG  | 22AWG  |
| 0.00163 | 0.00258 | 0.0041 | 0.00654 | 0.0103 | 0.0164 |

The voltage drop experienced by an engine will be equal to its current draw (amps) multiplied by twice the resistance of a single rail / wire from the point on the track back to the transformer. The American Flyer Service Manual indicates for steam engines, the maximum current draw at 12 volts a.c. can range from 1.75 to 2.3 amps when pulling 4 box cars. For diesels, the maximum current draw can range from 1.8 to 3.25 amps. For post war American Flyer steam engines, the maximum currents I measured on my collection of engines are between 1.6 and 2.5 amps when pulling 8 freight cars (6 gondolas, 1 box car, 1 TOFC). For a dual motor ALCO, I measured a maximum of 2.5 amps. An American Models Baldwin diesel with a can motor had a maximum current draw of 0.6 amps.

Based on the above, one can probably plan on a maximum current of about 2.5 amps. With a maximum track resistance difference of 0.25 ohms for desirable operation, this translates into a maximum voltage variation of  $2 \times 0.25 \times 2.5 = 1.25$  volts.

## 2. Cases

Figures 1 through 7 depict the seven cases and the resistances for three wire gauges and the three track resistances as calculated at points that are near the local maximum and minimum resistance values. The “Delta R” table provides the differences between the maximum and minimum resistances. Combinations of wire gauge and track resistance that resulted in a desirable “Delta R” of 0.25 ohms or less are highlighted in green. Marginal performance is highlighted in yellow, and Undesirable performance is highlighted in orange.

The data for all six wire gauges are presented in Appendix A.

For cases 1 through 6, the track oval was broken into 8 groups of 5 sections of track. The boundaries between groups are nodes labeled: 10, 12, 20, 23, 30, 34, 40, and 41. The transformer terminal is assigned node 0. Each group of tracks was modeled as a resistor with a label beginning with “RT\_” and ending with the labels of the two nodes at its end. In case 7, two of the groups are broken into two subgroups with node 60 midway between nodes 10 and 12, and node 61 midway between nodes 12 and 23. In this case, RT\_1060 and RT\_6012 replace RT\_1012, while RT\_1261 and RT\_6120 replace RT\_1220. The resistances of each track group (including low, medium, and high values) are presented in Table 3.

Table 3: Track group resistance

|         | sections | Resistance (ohms) |        |       |
|---------|----------|-------------------|--------|-------|
|         |          | L                 | M      | H     |
| RT_1012 | 5        | 0.125             | 0.375  | 0.75  |
| RT_1220 | 5        | 0.125             | 0.375  | 0.75  |
| RT_2023 | 5        | 0.125             | 0.375  | 0.75  |
| RT_2330 | 5        | 0.125             | 0.375  | 0.75  |
| RT_3034 | 5        | 0.125             | 0.375  | 0.75  |
| RT_3440 | 5        | 0.125             | 0.375  | 0.75  |
| RT_4041 | 5        | 0.125             | 0.375  | 0.75  |
| RT_4110 | 5        | 0.125             | 0.375  | 0.75  |
| RT_1060 | 2.5      | 0.0625            | 0.1875 | 0.375 |
| RT_6012 | 2.5      | 0.0625            | 0.1875 | 0.375 |
| RT_1261 | 2.5      | 0.0625            | 0.1875 | 0.375 |
| RT_6120 | 2.5      | 0.0625            | 0.1875 | 0.375 |

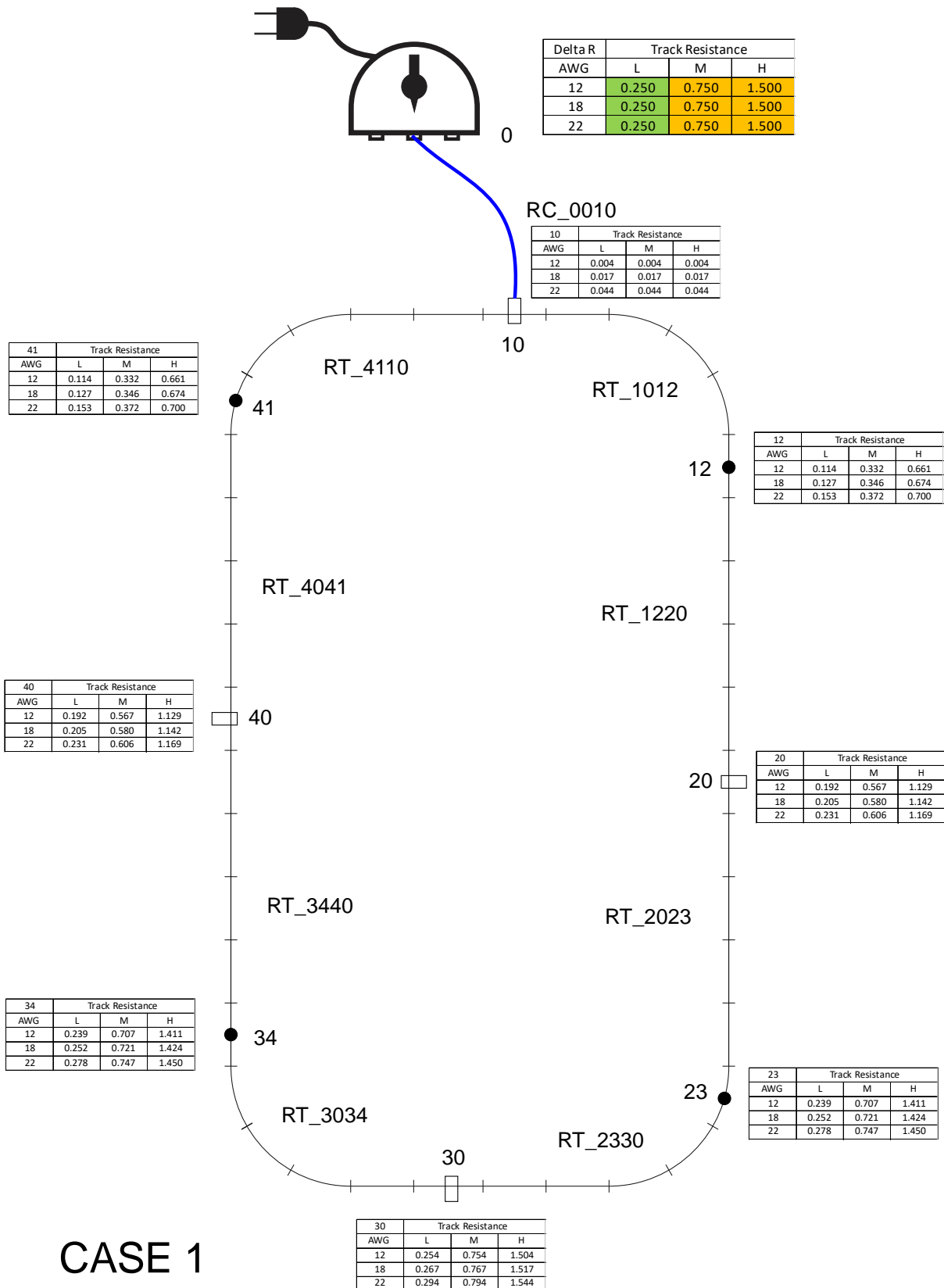
Copper wires are labeled with “RC\_” followed by the labels of the nodes they connect. Cases 6 and 7 have an additional node 50 used to connect wires together, but not associated with a track group. Details on all of the wires defined in all seven cases are provided in Table 4. All the wires are not used in any one case. Table 5 indicates which wires (cables) are used in each case and the total length of cable required.

Table 4: Resistance of copper wires (ohms)

| Wire    | length (in) | 12 AWG | 14 AWG | 16AWG  | 18AWG  | 20AWG  | 22AWG  |
|---------|-------------|--------|--------|--------|--------|--------|--------|
| RC_0010 | 32          | 0.0043 | 0.0069 | 0.0109 | 0.0174 | 0.0275 | 0.0437 |
| RC_1030 | 154         | 0.0209 | 0.0331 | 0.0526 | 0.0839 | 0.1322 | 0.2105 |
| RC_1020 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_2030 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_3040 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_4010 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_0020 | 134         | 0.0182 | 0.0288 | 0.0458 | 0.0730 | 0.1150 | 0.1831 |
| RC_0030 | 180         | 0.0245 | 0.0387 | 0.0615 | 0.0981 | 0.1545 | 0.2460 |
| RC_0040 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_0050 | 110         | 0.0149 | 0.0237 | 0.0376 | 0.0600 | 0.0944 | 0.1503 |
| RC_1050 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_2050 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_3050 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_4050 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_1250 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_2350 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_3450 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |
| RC_4150 | 80          | 0.0109 | 0.0172 | 0.0273 | 0.0436 | 0.0687 | 0.1093 |

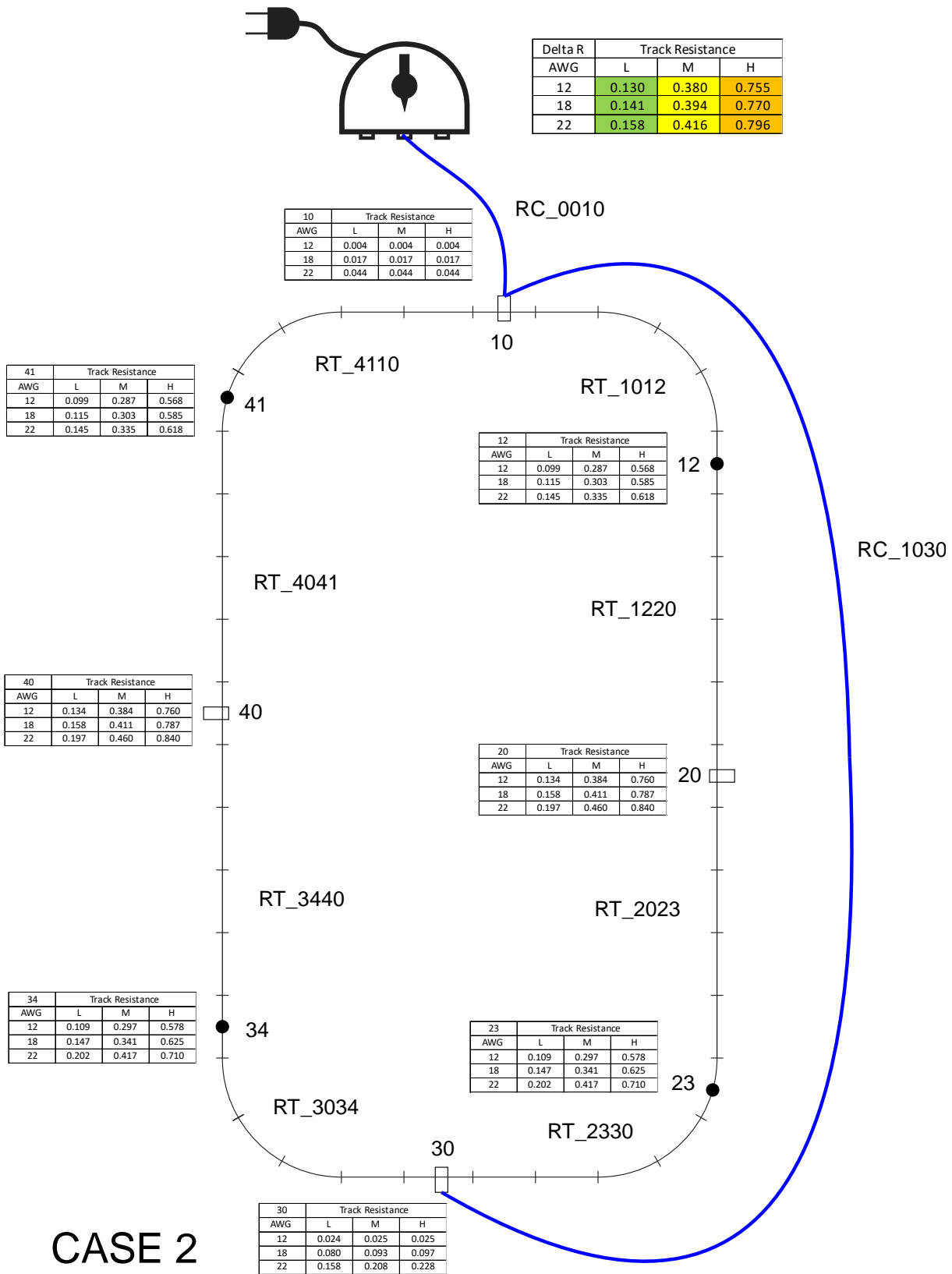
Table 5: Cable lengths and association with cases

|         | Cable (inches)       |        |        |        |        |        |        |
|---------|----------------------|--------|--------|--------|--------|--------|--------|
|         | Case 1               | Case 2 | Case 3 | Case 4 | Case 5 | Case 6 | Case 7 |
| RC_0010 | 32                   | 32     | 32     | 32     | 32     |        |        |
| RC_1030 |                      | 154    |        |        |        |        |        |
| RC_1020 |                      |        | 110    | 110    |        |        |        |
| RC_2030 |                      |        | 110    | 110    |        |        |        |
| RC_3040 |                      |        | 110    | 110    |        |        |        |
| RC_4010 |                      |        |        | 110    |        |        |        |
| RC_0020 |                      |        |        |        | 134    |        |        |
| RC_0030 |                      |        |        |        | 180    |        |        |
| RC_0040 |                      |        |        |        | 110    |        |        |
| RC_0050 |                      |        |        |        |        | 110    | 110    |
| RC_1050 |                      |        |        |        |        | 80     | 80     |
| RC_2050 |                      |        |        |        |        | 80     | 80     |
| RC_3050 |                      |        |        |        |        | 80     | 80     |
| RC_4050 |                      |        |        |        |        | 80     | 80     |
| RC_1250 |                      |        |        |        |        |        | 80     |
| RC_2350 |                      |        |        |        |        |        | 80     |
| RC_3450 |                      |        |        |        |        |        | 80     |
| RC_4150 |                      |        |        |        |        |        | 80     |
|         | Total Cable (inches) |        |        |        |        |        |        |
|         | Case 1               | Case 2 | Case 3 | Case 4 | Case 5 | Case 6 | Case 7 |
|         | 32                   | 186    | 362    | 472    | 456    | 430    | 750    |



# CASE 1

Figure 1: Case 1



CASE 2

Figure 2: Case 2



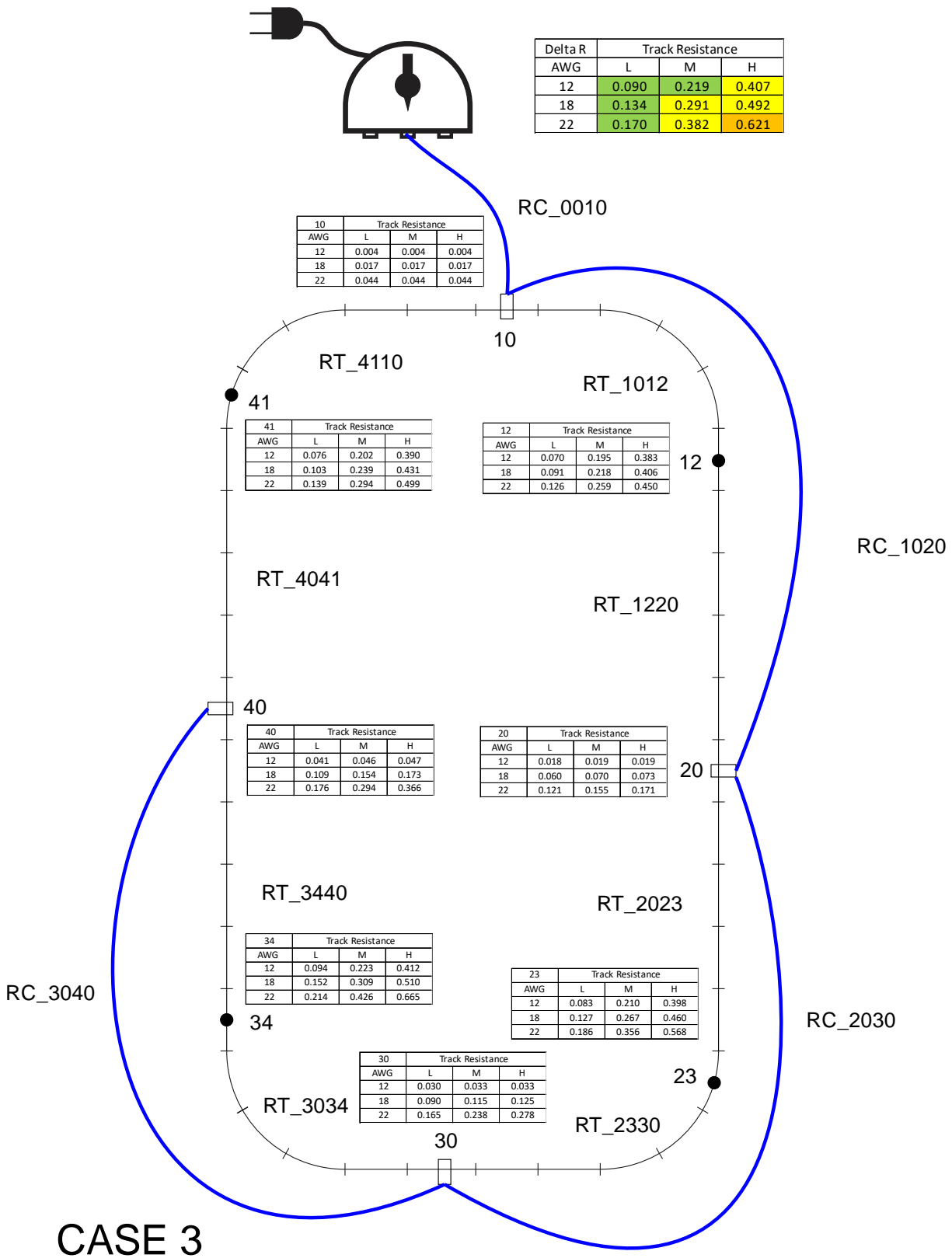


Figure 3: Case 3

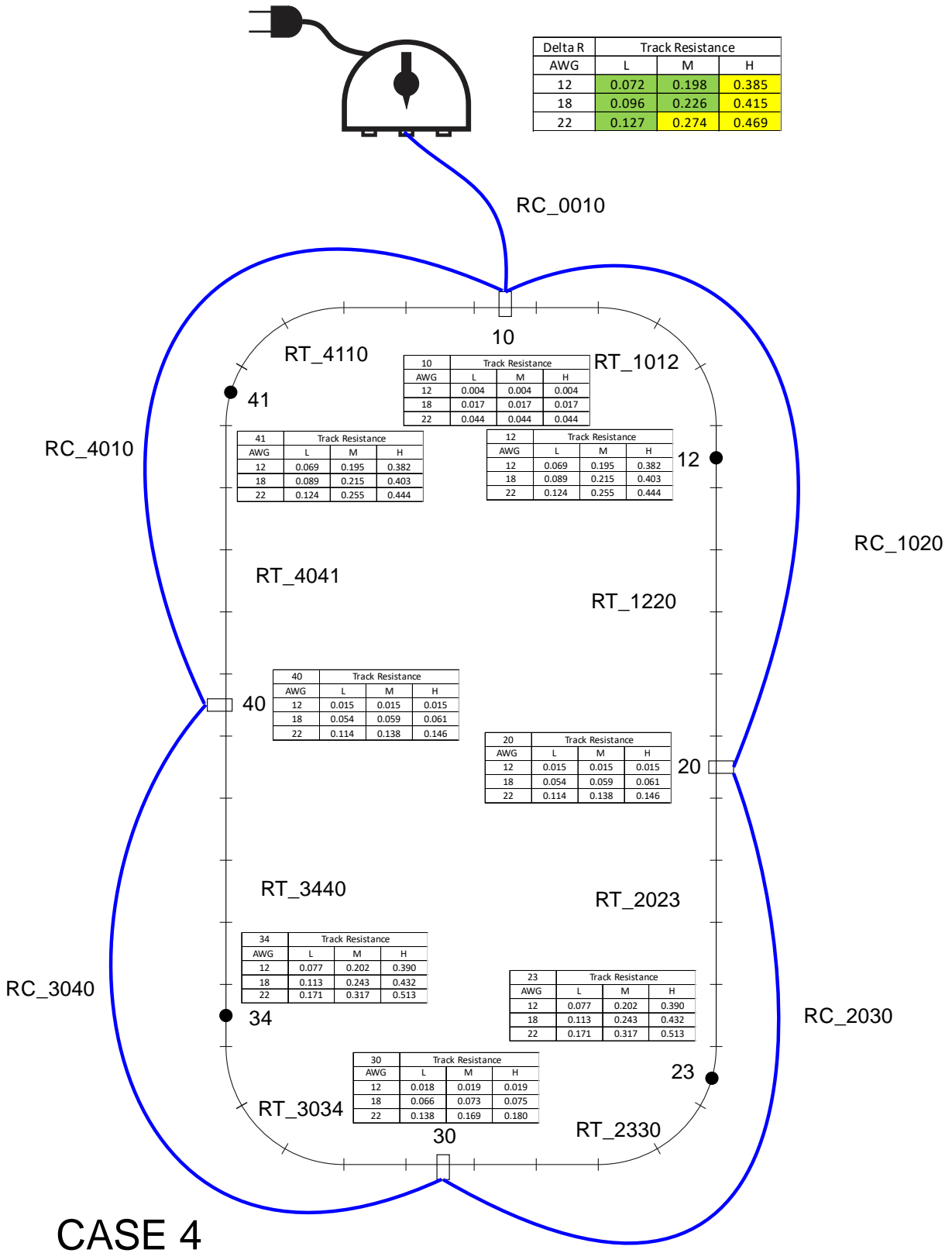
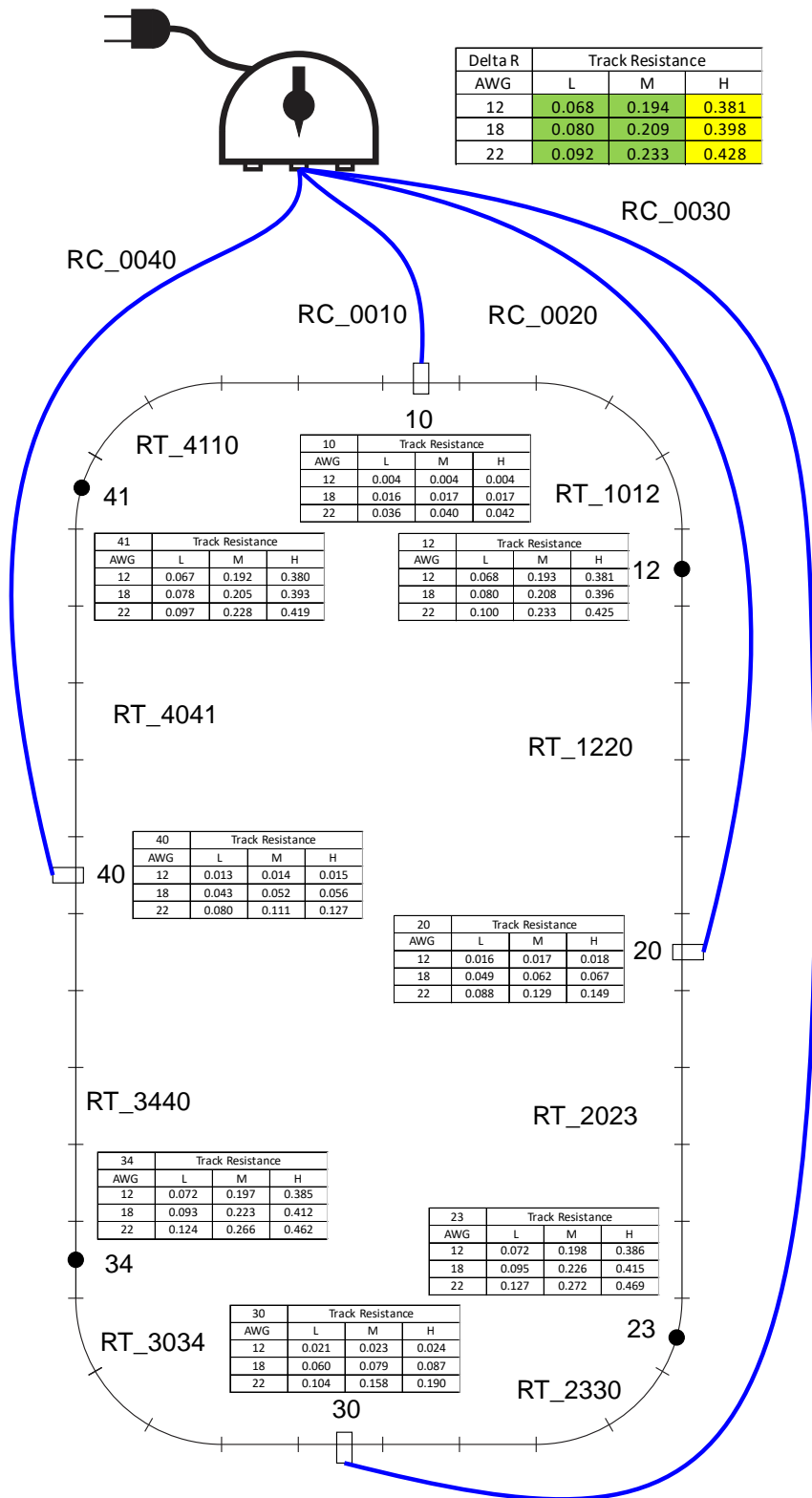
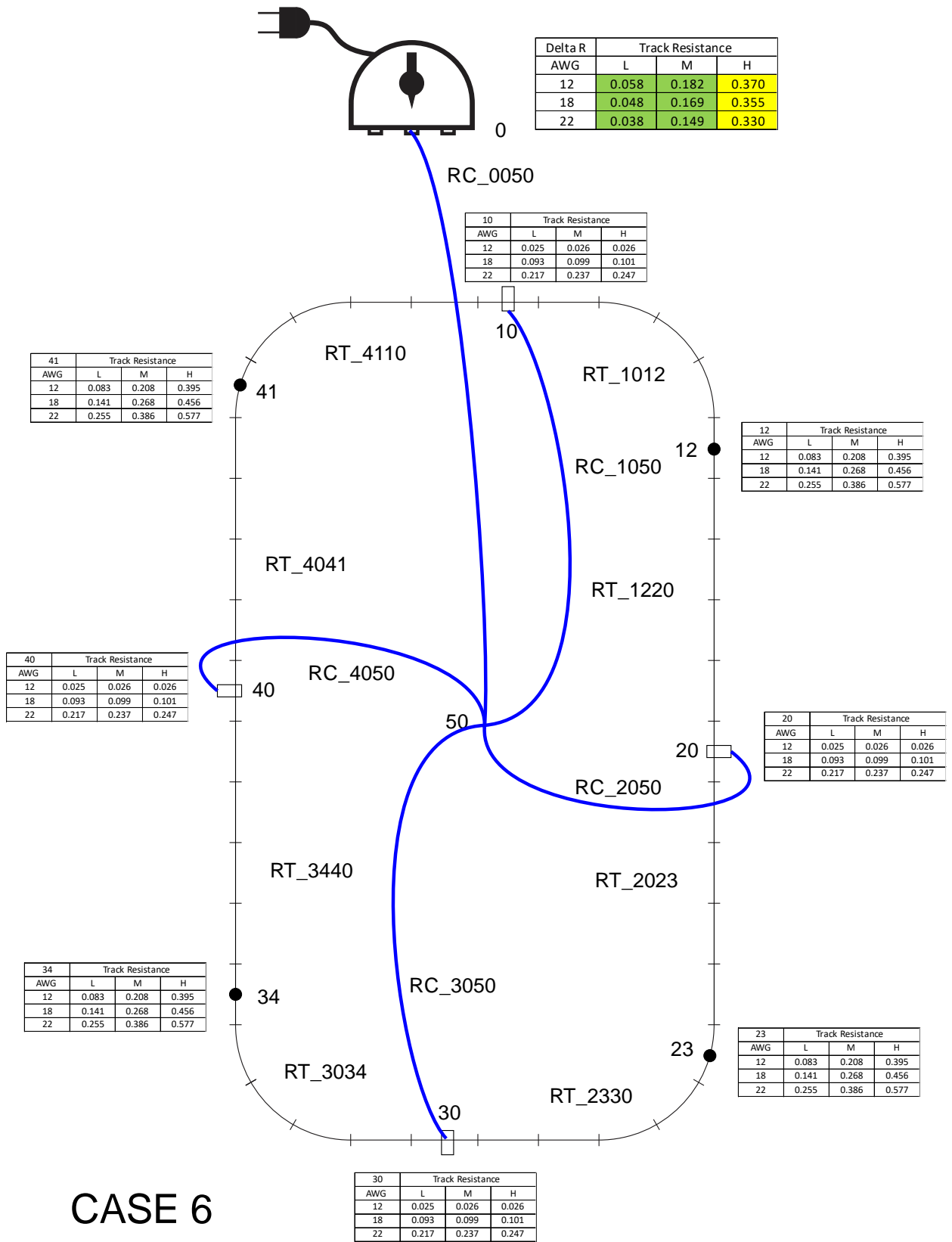


Figure 4: Case 4



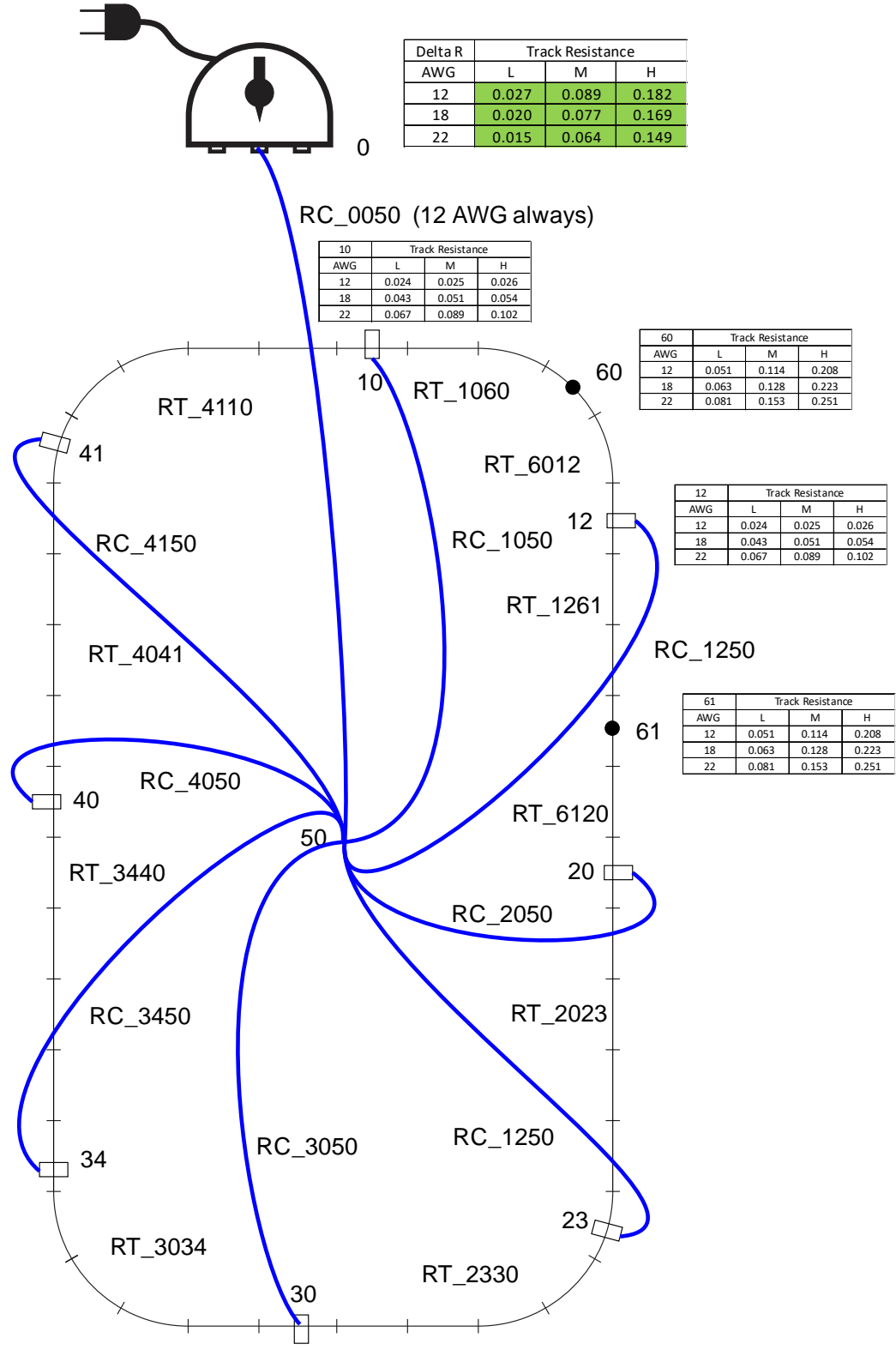
# CASE 5

Figure 5: Case 5



# CASE 6

Figure 6: Case 6



# CASE 7

Figure 7: Case 7



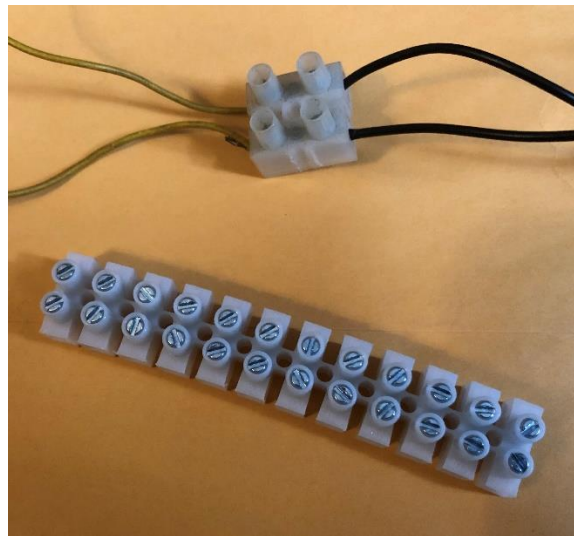
### 3. Observations and Recommendations

In examining the “Delta R” tables for all seven cases it is apparent that minimizing track resistance has a greater impact on acceptability than increasing the size (lower AWG) of the copper wire. Similarly, adding more connections to the track (1 for Case 1, 2 for Case 2, 4 for Cases 3-6, and 8 for Case 7) has a greater impact than increasing copper wire size. In fact in Case 7, acceptable performance is achieved with the smallest wire (22 AWG).

Based on the results of this analysis, I recommend using a “star” type wiring configuration as depicted in Cases 6 and 7. Key to minimizing the “Delta R” is keeping all of the wires from the common distribution point to the track roughly the same length and the same gauge as well as having track-wire connections no more than 5 track sections apart (as in Case 7). Although of lesser importance, I recommend using 18 AWG wire or larger to reduce the average resistance.

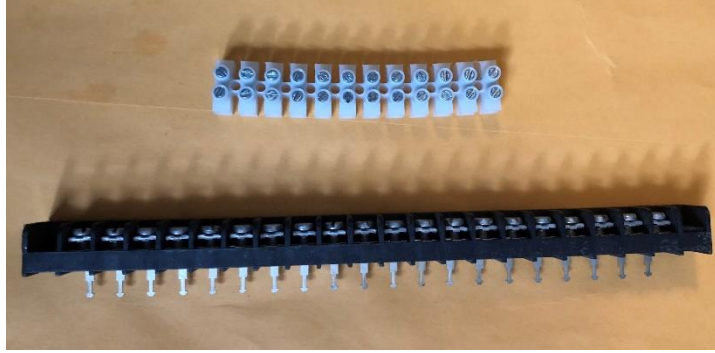
To make it easier to maintain the layout while maintaining a good electrical connection between the wire and track, I recommend soldering the wire directly to the underside of each rail. I recommend soldering about a 9 inch length of 22 AWG wire to the rail. While one would still likely need a high wattage soldering iron (40 watts or more) or a soldering gun, it is easier to solder a 22 AWG wire to a rail than a wire of greater size. Make sure the solder joint area on the track is clean and corrosion free.

Underneath the train table, you can connect the 22 AWG wire to a larger gauge wire using a 2 pole European style terminal block as depicted in Figure 8. The European style terminal blocks usually are purchased with 8 or more poles; but they are easily cut down to size.



*Figure 8: European Style Terminal Blocks*

There are many options for the common distribution point. I generally recommend using either the European style Terminal Blocks or a feed through Terminal Block as depicted in Figure 9. You can use one terminal block for each of the two rails. With the feed through Terminal Block, all the terminals can be electrically connected by soldering a bare solid copper wire across all the terminal pole leads; the track and transformer wire are attached using the screws on top. For the European style Terminal Block, you can use solid wire to connect all the terminal poles on one side and connect the track and transformer wire on the other side. There are many other possible solutions that will work just as well.



*Figure 9: Terminal Block Examples*



## Appendix A: Data

Resistance to transformer (ohms) from Node

| CASE | Track R | AWG | 10    | 12    | 20    | 23    | 30    | 34    | 40    | 41    | Average R | Std Deviation | Greatest R | Smallest R | Delta R |
|------|---------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-----------|---------------|------------|------------|---------|
| 1    | 0.025   | 12  | 0.004 | 0.114 | 0.192 | 0.239 | 0.254 | 0.239 | 0.192 | 0.114 | 0.168     | 0.086         | 0.254      | 0.004      | 0.250   |
| 1    | 0.025   | 14  | 0.007 | 0.116 | 0.194 | 0.241 | 0.257 | 0.241 | 0.194 | 0.116 | 0.171     | 0.086         | 0.257      | 0.007      | 0.250   |
| 1    | 0.025   | 16  | 0.011 | 0.120 | 0.198 | 0.245 | 0.261 | 0.245 | 0.198 | 0.120 | 0.175     | 0.086         | 0.261      | 0.011      | 0.250   |
| 1    | 0.025   | 18  | 0.017 | 0.127 | 0.205 | 0.252 | 0.267 | 0.252 | 0.205 | 0.127 | 0.182     | 0.086         | 0.267      | 0.017      | 0.250   |
| 1    | 0.025   | 20  | 0.027 | 0.137 | 0.215 | 0.262 | 0.277 | 0.262 | 0.215 | 0.137 | 0.192     | 0.086         | 0.277      | 0.027      | 0.250   |
| 1    | 0.025   | 22  | 0.044 | 0.153 | 0.231 | 0.278 | 0.294 | 0.278 | 0.231 | 0.153 | 0.208     | 0.086         | 0.294      | 0.044      | 0.250   |
| 1    | 0.075   | 12  | 0.004 | 0.332 | 0.567 | 0.707 | 0.754 | 0.707 | 0.567 | 0.332 | 0.497     | 0.257         | 0.754      | 0.004      | 0.750   |
| 1    | 0.075   | 14  | 0.007 | 0.335 | 0.569 | 0.710 | 0.757 | 0.710 | 0.569 | 0.335 | 0.499     | 0.257         | 0.757      | 0.007      | 0.750   |
| 1    | 0.075   | 16  | 0.011 | 0.339 | 0.573 | 0.714 | 0.761 | 0.714 | 0.573 | 0.339 | 0.503     | 0.257         | 0.761      | 0.011      | 0.750   |
| 1    | 0.075   | 18  | 0.017 | 0.346 | 0.580 | 0.721 | 0.767 | 0.721 | 0.580 | 0.346 | 0.510     | 0.257         | 0.767      | 0.017      | 0.750   |
| 1    | 0.075   | 20  | 0.027 | 0.356 | 0.590 | 0.731 | 0.777 | 0.731 | 0.590 | 0.356 | 0.520     | 0.257         | 0.777      | 0.027      | 0.750   |
| 1    | 0.075   | 22  | 0.044 | 0.372 | 0.606 | 0.747 | 0.794 | 0.747 | 0.606 | 0.372 | 0.536     | 0.257         | 0.794      | 0.044      | 0.750   |
| 1    | 0.15    | 12  | 0.004 | 0.661 | 1.129 | 1.411 | 1.504 | 1.411 | 1.129 | 0.661 | 0.989     | 0.513         | 1.504      | 0.004      | 1.500   |
| 1    | 0.15    | 14  | 0.007 | 0.663 | 1.132 | 1.413 | 1.507 | 1.413 | 1.132 | 0.663 | 0.991     | 0.513         | 1.507      | 0.007      | 1.500   |
| 1    | 0.15    | 16  | 0.011 | 0.667 | 1.136 | 1.417 | 1.511 | 1.417 | 1.136 | 0.667 | 0.995     | 0.513         | 1.511      | 0.011      | 1.500   |
| 1    | 0.15    | 18  | 0.017 | 0.674 | 1.142 | 1.424 | 1.517 | 1.424 | 1.142 | 0.674 | 1.002     | 0.513         | 1.517      | 0.017      | 1.500   |
| 1    | 0.15    | 20  | 0.027 | 0.684 | 1.152 | 1.434 | 1.527 | 1.434 | 1.152 | 0.684 | 1.012     | 0.513         | 1.527      | 0.027      | 1.500   |
| 1    | 0.15    | 22  | 0.044 | 0.700 | 1.169 | 1.450 | 1.544 | 1.450 | 1.169 | 0.700 | 1.028     | 0.513         | 1.544      | 0.044      | 1.500   |
| 2    | 0.025   | 12  | 0.004 | 0.099 | 0.134 | 0.109 | 0.024 | 0.109 | 0.134 | 0.099 | 0.089     | 0.049         | 0.134      | 0.004      | 0.130   |
| 2    | 0.025   | 14  | 0.007 | 0.102 | 0.139 | 0.117 | 0.036 | 0.117 | 0.139 | 0.102 | 0.095     | 0.048         | 0.139      | 0.007      | 0.132   |
| 2    | 0.025   | 16  | 0.011 | 0.107 | 0.147 | 0.129 | 0.054 | 0.129 | 0.147 | 0.107 | 0.104     | 0.048         | 0.147      | 0.011      | 0.136   |
| 2    | 0.025   | 18  | 0.017 | 0.115 | 0.158 | 0.147 | 0.080 | 0.147 | 0.158 | 0.115 | 0.117     | 0.048         | 0.158      | 0.017      | 0.141   |
| 2    | 0.025   | 20  | 0.027 | 0.127 | 0.174 | 0.170 | 0.114 | 0.170 | 0.174 | 0.127 | 0.135     | 0.050         | 0.174      | 0.027      | 0.147   |
| 2    | 0.025   | 22  | 0.044 | 0.145 | 0.197 | 0.202 | 0.158 | 0.202 | 0.197 | 0.145 | 0.161     | 0.054         | 0.202      | 0.044      | 0.158   |
| 2    | 0.075   | 12  | 0.004 | 0.287 | 0.384 | 0.297 | 0.025 | 0.297 | 0.384 | 0.287 | 0.246     | 0.148         | 0.384      | 0.004      | 0.380   |
| 2    | 0.075   | 14  | 0.007 | 0.290 | 0.390 | 0.306 | 0.039 | 0.306 | 0.390 | 0.290 | 0.252     | 0.148         | 0.390      | 0.007      | 0.383   |
| 2    | 0.075   | 16  | 0.011 | 0.295 | 0.398 | 0.320 | 0.060 | 0.320 | 0.398 | 0.295 | 0.262     | 0.146         | 0.398      | 0.011      | 0.387   |
| 2    | 0.075   | 18  | 0.017 | 0.303 | 0.411 | 0.341 | 0.093 | 0.341 | 0.411 | 0.303 | 0.278     | 0.145         | 0.411      | 0.017      | 0.394   |
| 2    | 0.075   | 20  | 0.027 | 0.316 | 0.431 | 0.372 | 0.140 | 0.372 | 0.431 | 0.316 | 0.300     | 0.144         | 0.431      | 0.027      | 0.403   |
| 2    | 0.075   | 22  | 0.044 | 0.335 | 0.460 | 0.417 | 0.208 | 0.417 | 0.460 | 0.335 | 0.335     | 0.144         | 0.460      | 0.044      | 0.416   |
| 2    | 0.15    | 12  | 0.004 | 0.568 | 0.760 | 0.578 | 0.025 | 0.578 | 0.760 | 0.568 | 0.480     | 0.299         | 0.760      | 0.004      | 0.755   |
| 2    | 0.15    | 14  | 0.007 | 0.571 | 0.765 | 0.588 | 0.039 | 0.588 | 0.765 | 0.571 | 0.487     | 0.298         | 0.765      | 0.007      | 0.758   |
| 2    | 0.15    | 16  | 0.011 | 0.577 | 0.774 | 0.602 | 0.062 | 0.602 | 0.774 | 0.577 | 0.497     | 0.296         | 0.774      | 0.011      | 0.763   |
| 2    | 0.15    | 18  | 0.017 | 0.585 | 0.787 | 0.625 | 0.097 | 0.625 | 0.787 | 0.585 | 0.514     | 0.294         | 0.787      | 0.017      | 0.770   |

Resistance to transformer (ohms) from Node

| CASE | Track R | AWG | 10    | 12    | 20    | 23    | 30    | 34    | 40    | 41    | Std       |           | Delta R |            |            |
|------|---------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-----------|-----------|---------|------------|------------|
|      |         |     |       |       |       |       |       |       |       |       | Average R | Deviation |         | Greatest R | Smallest R |
| 2    | 0.15    | 20  | 0.027 | 0.598 | 0.808 | 0.658 | 0.149 | 0.658 | 0.808 | 0.598 | 0.538     | 0.291     | 0.808   | 0.027      | 0.780      |
| 2    | 0.15    | 22  | 0.044 | 0.618 | 0.840 | 0.710 | 0.228 | 0.710 | 0.840 | 0.618 | 0.576     | 0.289     | 0.840   | 0.044      | 0.796      |
| 3    | 0.025   | 12  | 0.004 | 0.070 | 0.018 | 0.083 | 0.030 | 0.094 | 0.041 | 0.076 | 0.052     | 0.033     | 0.094   | 0.004      | 0.090      |
| 3    | 0.025   | 14  | 0.007 | 0.074 | 0.027 | 0.093 | 0.044 | 0.109 | 0.058 | 0.082 | 0.062     | 0.034     | 0.109   | 0.007      | 0.102      |
| 3    | 0.025   | 16  | 0.011 | 0.081 | 0.041 | 0.107 | 0.064 | 0.128 | 0.081 | 0.091 | 0.075     | 0.037     | 0.128   | 0.011      | 0.117      |
| 3    | 0.025   | 18  | 0.017 | 0.091 | 0.060 | 0.127 | 0.090 | 0.152 | 0.109 | 0.103 | 0.094     | 0.041     | 0.152   | 0.017      | 0.134      |
| 3    | 0.025   | 20  | 0.027 | 0.105 | 0.086 | 0.152 | 0.123 | 0.180 | 0.140 | 0.118 | 0.116     | 0.046     | 0.180   | 0.027      | 0.152      |
| 3    | 0.025   | 22  | 0.044 | 0.126 | 0.121 | 0.186 | 0.165 | 0.214 | 0.176 | 0.139 | 0.146     | 0.052     | 0.214   | 0.044      | 0.170      |
| 3    | 0.075   | 12  | 0.004 | 0.195 | 0.019 | 0.210 | 0.033 | 0.223 | 0.046 | 0.202 | 0.116     | 0.098     | 0.223   | 0.004      | 0.219      |
| 3    | 0.075   | 14  | 0.007 | 0.200 | 0.029 | 0.222 | 0.050 | 0.242 | 0.070 | 0.210 | 0.129     | 0.098     | 0.242   | 0.007      | 0.235      |
| 3    | 0.075   | 16  | 0.011 | 0.207 | 0.045 | 0.240 | 0.077 | 0.270 | 0.105 | 0.222 | 0.147     | 0.099     | 0.270   | 0.011      | 0.259      |
| 3    | 0.075   | 18  | 0.017 | 0.218 | 0.070 | 0.267 | 0.115 | 0.309 | 0.154 | 0.239 | 0.174     | 0.102     | 0.309   | 0.017      | 0.291      |
| 3    | 0.075   | 20  | 0.027 | 0.234 | 0.104 | 0.304 | 0.167 | 0.360 | 0.216 | 0.262 | 0.209     | 0.108     | 0.360   | 0.027      | 0.332      |
| 3    | 0.075   | 22  | 0.044 | 0.259 | 0.155 | 0.356 | 0.238 | 0.426 | 0.294 | 0.294 | 0.258     | 0.118     | 0.426   | 0.044      | 0.382      |
| 3    | 0.15    | 12  | 0.004 | 0.383 | 0.019 | 0.398 | 0.033 | 0.412 | 0.047 | 0.390 | 0.211     | 0.198     | 0.412   | 0.004      | 0.407      |
| 3    | 0.15    | 14  | 0.007 | 0.388 | 0.030 | 0.410 | 0.052 | 0.432 | 0.074 | 0.399 | 0.224     | 0.197     | 0.432   | 0.007      | 0.425      |
| 3    | 0.15    | 16  | 0.011 | 0.395 | 0.047 | 0.430 | 0.081 | 0.463 | 0.113 | 0.412 | 0.244     | 0.197     | 0.463   | 0.011      | 0.452      |
| 3    | 0.15    | 18  | 0.017 | 0.406 | 0.073 | 0.460 | 0.125 | 0.510 | 0.173 | 0.431 | 0.274     | 0.197     | 0.510   | 0.017      | 0.492      |
| 3    | 0.15    | 20  | 0.027 | 0.424 | 0.112 | 0.503 | 0.187 | 0.574 | 0.254 | 0.459 | 0.318     | 0.200     | 0.574   | 0.027      | 0.547      |
| 3    | 0.15    | 22  | 0.044 | 0.450 | 0.171 | 0.568 | 0.278 | 0.665 | 0.366 | 0.499 | 0.380     | 0.208     | 0.665   | 0.044      | 0.621      |
| 4    | 0.025   | 12  | 0.004 | 0.069 | 0.015 | 0.077 | 0.018 | 0.077 | 0.015 | 0.069 | 0.043     | 0.032     | 0.077   | 0.004      | 0.072      |
| 4    | 0.025   | 14  | 0.007 | 0.073 | 0.023 | 0.084 | 0.028 | 0.084 | 0.023 | 0.073 | 0.050     | 0.032     | 0.084   | 0.007      | 0.077      |
| 4    | 0.025   | 16  | 0.011 | 0.080 | 0.035 | 0.096 | 0.044 | 0.096 | 0.035 | 0.080 | 0.060     | 0.032     | 0.096   | 0.011      | 0.085      |
| 4    | 0.025   | 18  | 0.017 | 0.089 | 0.054 | 0.113 | 0.066 | 0.113 | 0.054 | 0.089 | 0.074     | 0.033     | 0.113   | 0.017      | 0.096      |
| 4    | 0.025   | 20  | 0.027 | 0.103 | 0.079 | 0.137 | 0.096 | 0.137 | 0.079 | 0.103 | 0.095     | 0.035     | 0.137   | 0.027      | 0.110      |
| 4    | 0.025   | 22  | 0.044 | 0.124 | 0.114 | 0.171 | 0.138 | 0.171 | 0.114 | 0.124 | 0.125     | 0.040     | 0.171   | 0.044      | 0.127      |
| 4    | 0.075   | 12  | 0.004 | 0.195 | 0.015 | 0.202 | 0.019 | 0.202 | 0.015 | 0.195 | 0.106     | 0.099     | 0.202   | 0.004      | 0.198      |
| 4    | 0.075   | 14  | 0.007 | 0.199 | 0.024 | 0.210 | 0.030 | 0.210 | 0.024 | 0.199 | 0.113     | 0.098     | 0.210   | 0.007      | 0.203      |
| 4    | 0.075   | 16  | 0.011 | 0.205 | 0.038 | 0.223 | 0.047 | 0.223 | 0.038 | 0.205 | 0.124     | 0.097     | 0.223   | 0.011      | 0.212      |
| 4    | 0.075   | 18  | 0.017 | 0.215 | 0.059 | 0.243 | 0.073 | 0.243 | 0.059 | 0.215 | 0.141     | 0.097     | 0.243   | 0.017      | 0.226      |
| 4    | 0.075   | 20  | 0.027 | 0.231 | 0.090 | 0.273 | 0.111 | 0.273 | 0.090 | 0.231 | 0.166     | 0.096     | 0.273   | 0.027      | 0.245      |
| 4    | 0.075   | 22  | 0.044 | 0.255 | 0.138 | 0.317 | 0.169 | 0.317 | 0.138 | 0.255 | 0.204     | 0.098     | 0.317   | 0.044      | 0.274      |
| 4    | 0.15    | 12  | 0.004 | 0.382 | 0.015 | 0.390 | 0.019 | 0.390 | 0.015 | 0.382 | 0.200     | 0.199     | 0.390   | 0.004      | 0.385      |
| 4    | 0.15    | 14  | 0.007 | 0.386 | 0.024 | 0.398 | 0.030 | 0.398 | 0.024 | 0.386 | 0.207     | 0.198     | 0.398   | 0.007      | 0.391      |

Resistance to transformer (ohms) from Node

| CASE | Track R | AWG | 10    | 12    | 20    | 23    | 30    | 34    | 40    | 41    | Average R | Std Deviation | Greatest R | Smallest R | Delta R |
|------|---------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-----------|---------------|------------|------------|---------|
| 4    | 0.15    | 16  | 0.011 | 0.393 | 0.038 | 0.411 | 0.048 | 0.411 | 0.038 | 0.393 | 0.218     | 0.197         | 0.411      | 0.011      | 0.400   |
| 4    | 0.15    | 18  | 0.017 | 0.403 | 0.061 | 0.432 | 0.075 | 0.432 | 0.061 | 0.403 | 0.236     | 0.196         | 0.432      | 0.017      | 0.415   |
| 4    | 0.15    | 20  | 0.027 | 0.419 | 0.094 | 0.464 | 0.116 | 0.464 | 0.094 | 0.419 | 0.262     | 0.194         | 0.464      | 0.027      | 0.436   |
| 4    | 0.15    | 22  | 0.044 | 0.444 | 0.146 | 0.513 | 0.180 | 0.513 | 0.146 | 0.444 | 0.304     | 0.192         | 0.513      | 0.044      | 0.469   |
| 5    | 0.025   | 12  | 0.004 | 0.068 | 0.016 | 0.072 | 0.021 | 0.072 | 0.013 | 0.067 | 0.042     | 0.030         | 0.072      | 0.004      | 0.068   |
| 5    | 0.025   | 14  | 0.007 | 0.070 | 0.024 | 0.077 | 0.030 | 0.076 | 0.020 | 0.069 | 0.047     | 0.029         | 0.077      | 0.007      | 0.071   |
| 5    | 0.025   | 16  | 0.010 | 0.074 | 0.034 | 0.085 | 0.043 | 0.083 | 0.030 | 0.073 | 0.054     | 0.028         | 0.085      | 0.010      | 0.075   |
| 5    | 0.025   | 18  | 0.016 | 0.080 | 0.049 | 0.095 | 0.060 | 0.093 | 0.043 | 0.078 | 0.064     | 0.028         | 0.095      | 0.016      | 0.080   |
| 5    | 0.025   | 20  | 0.024 | 0.088 | 0.066 | 0.109 | 0.080 | 0.106 | 0.059 | 0.086 | 0.077     | 0.028         | 0.109      | 0.024      | 0.085   |
| 5    | 0.025   | 22  | 0.036 | 0.100 | 0.088 | 0.127 | 0.104 | 0.124 | 0.080 | 0.097 | 0.095     | 0.029         | 0.127      | 0.036      | 0.092   |
| 5    | 0.075   | 12  | 0.004 | 0.193 | 0.017 | 0.198 | 0.023 | 0.197 | 0.014 | 0.192 | 0.105     | 0.097         | 0.198      | 0.004      | 0.194   |
| 5    | 0.075   | 14  | 0.007 | 0.196 | 0.027 | 0.204 | 0.035 | 0.202 | 0.022 | 0.195 | 0.111     | 0.095         | 0.204      | 0.007      | 0.197   |
| 5    | 0.075   | 16  | 0.011 | 0.201 | 0.041 | 0.213 | 0.053 | 0.211 | 0.034 | 0.199 | 0.120     | 0.092         | 0.213      | 0.011      | 0.202   |
| 5    | 0.075   | 18  | 0.017 | 0.208 | 0.062 | 0.226 | 0.079 | 0.223 | 0.052 | 0.205 | 0.134     | 0.089         | 0.226      | 0.017      | 0.209   |
| 5    | 0.075   | 20  | 0.026 | 0.218 | 0.090 | 0.245 | 0.113 | 0.241 | 0.077 | 0.214 | 0.153     | 0.086         | 0.245      | 0.026      | 0.219   |
| 5    | 0.075   | 22  | 0.040 | 0.233 | 0.129 | 0.272 | 0.158 | 0.266 | 0.111 | 0.228 | 0.180     | 0.083         | 0.272      | 0.040      | 0.233   |
| 5    | 0.15    | 12  | 0.004 | 0.381 | 0.018 | 0.386 | 0.024 | 0.385 | 0.015 | 0.380 | 0.199     | 0.197         | 0.386      | 0.004      | 0.381   |
| 5    | 0.15    | 14  | 0.007 | 0.384 | 0.028 | 0.391 | 0.037 | 0.390 | 0.023 | 0.382 | 0.205     | 0.194         | 0.391      | 0.007      | 0.385   |
| 5    | 0.15    | 16  | 0.011 | 0.389 | 0.043 | 0.401 | 0.057 | 0.399 | 0.036 | 0.387 | 0.215     | 0.191         | 0.401      | 0.011      | 0.390   |
| 5    | 0.15    | 18  | 0.017 | 0.396 | 0.067 | 0.415 | 0.087 | 0.412 | 0.056 | 0.393 | 0.231     | 0.187         | 0.415      | 0.017      | 0.398   |
| 5    | 0.15    | 20  | 0.027 | 0.408 | 0.100 | 0.437 | 0.129 | 0.432 | 0.084 | 0.403 | 0.253     | 0.182         | 0.437      | 0.027      | 0.410   |
| 5    | 0.15    | 22  | 0.042 | 0.425 | 0.149 | 0.469 | 0.190 | 0.462 | 0.127 | 0.419 | 0.285     | 0.175         | 0.469      | 0.042      | 0.428   |
| 6    | 0.025   | 12  | 0.025 | 0.083 | 0.025 | 0.083 | 0.025 | 0.083 | 0.025 | 0.083 | 0.054     | 0.031         | 0.083      | 0.025      | 0.058   |
| 6    | 0.025   | 14  | 0.039 | 0.094 | 0.039 | 0.094 | 0.039 | 0.094 | 0.039 | 0.094 | 0.067     | 0.030         | 0.094      | 0.039      | 0.055   |
| 6    | 0.025   | 16  | 0.060 | 0.113 | 0.060 | 0.113 | 0.060 | 0.113 | 0.060 | 0.113 | 0.086     | 0.028         | 0.113      | 0.060      | 0.052   |
| 6    | 0.025   | 18  | 0.093 | 0.141 | 0.093 | 0.141 | 0.093 | 0.141 | 0.093 | 0.141 | 0.117     | 0.026         | 0.141      | 0.093      | 0.048   |
| 6    | 0.025   | 20  | 0.142 | 0.185 | 0.142 | 0.185 | 0.142 | 0.185 | 0.142 | 0.185 | 0.164     | 0.023         | 0.185      | 0.142      | 0.043   |
| 6    | 0.025   | 22  | 0.217 | 0.255 | 0.217 | 0.255 | 0.217 | 0.255 | 0.217 | 0.255 | 0.236     | 0.020         | 0.255      | 0.217      | 0.038   |
| 6    | 0.075   | 12  | 0.026 | 0.208 | 0.026 | 0.208 | 0.026 | 0.208 | 0.026 | 0.208 | 0.117     | 0.097         | 0.208      | 0.026      | 0.182   |
| 6    | 0.075   | 14  | 0.040 | 0.220 | 0.040 | 0.220 | 0.040 | 0.220 | 0.040 | 0.220 | 0.130     | 0.096         | 0.220      | 0.040      | 0.179   |
| 6    | 0.075   | 16  | 0.063 | 0.238 | 0.063 | 0.238 | 0.063 | 0.238 | 0.063 | 0.238 | 0.151     | 0.094         | 0.238      | 0.063      | 0.175   |
| 6    | 0.075   | 18  | 0.099 | 0.268 | 0.099 | 0.268 | 0.099 | 0.268 | 0.099 | 0.268 | 0.184     | 0.090         | 0.268      | 0.099      | 0.169   |
| 6    | 0.075   | 20  | 0.153 | 0.314 | 0.153 | 0.314 | 0.153 | 0.314 | 0.153 | 0.314 | 0.233     | 0.086         | 0.314      | 0.153      | 0.160   |
| 6    | 0.075   | 22  | 0.237 | 0.386 | 0.237 | 0.386 | 0.237 | 0.386 | 0.237 | 0.386 | 0.312     | 0.080         | 0.386      | 0.237      | 0.149   |

Resistance to transformer (ohms) from Node

| CASE | Track R | AWG | 10    | 12    | 20    | 23    | 30    | 34    | 40    | 41    | Average R | Std Deviation | Greatest R | Smallest R | Delta R |
|------|---------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-----------|---------------|------------|------------|---------|
| 6    | 0.15    | 12  | 0.026 | 0.395 | 0.026 | 0.395 | 0.026 | 0.395 | 0.026 | 0.395 | 0.210     | 0.198         | 0.395      | 0.026      | 0.370   |
| 6    | 0.15    | 14  | 0.040 | 0.407 | 0.040 | 0.407 | 0.040 | 0.407 | 0.040 | 0.407 | 0.224     | 0.196         | 0.407      | 0.040      | 0.367   |
| 6    | 0.15    | 16  | 0.064 | 0.426 | 0.064 | 0.426 | 0.064 | 0.426 | 0.064 | 0.426 | 0.245     | 0.194         | 0.426      | 0.064      | 0.362   |
| 6    | 0.15    | 18  | 0.101 | 0.456 | 0.101 | 0.456 | 0.101 | 0.456 | 0.101 | 0.456 | 0.279     | 0.190         | 0.456      | 0.101      | 0.355   |
| 6    | 0.15    | 20  | 0.158 | 0.502 | 0.158 | 0.502 | 0.158 | 0.502 | 0.158 | 0.502 | 0.330     | 0.184         | 0.502      | 0.158      | 0.345   |
| 6    | 0.15    | 22  | 0.247 | 0.577 | 0.247 | 0.577 | 0.247 | 0.577 | 0.247 | 0.577 | 0.412     | 0.176         | 0.577      | 0.247      | 0.330   |

CASE 7

| Resistance to transformer (ohms) from Node |     |       |       |       |       |           |               |            |            |         |
|--|-----|-------|-------|-------|-------|-----------|---------------|------------|------------|---------|
| Track R                                    | AWG | 10    | 60    | 12    | 61    | Average R | Std Deviation | Greatest R | Smallest R | Delta R |
| 0.025                                      | 12  | 0.024 | 0.051 | 0.024 | 0.051 | 0.038     | 0.016         | 0.051      | 0.024      | 0.027   |
| 0.025                                      | 14  | 0.029 | 0.054 | 0.029 | 0.054 | 0.041     | 0.014         | 0.054      | 0.029      | 0.025   |
| 0.025                                      | 16  | 0.035 | 0.058 | 0.035 | 0.058 | 0.046     | 0.013         | 0.058      | 0.035      | 0.023   |
| 0.025                                      | 18  | 0.043 | 0.063 | 0.043 | 0.063 | 0.053     | 0.012         | 0.063      | 0.043      | 0.020   |
| 0.025                                      | 20  | 0.053 | 0.071 | 0.053 | 0.071 | 0.062     | 0.010         | 0.071      | 0.053      | 0.017   |
| 0.025                                      | 22  | 0.067 | 0.081 | 0.067 | 0.081 | 0.074     | 0.009         | 0.081      | 0.067      | 0.015   |
| 0.075                                      | 12  | 0.025 | 0.114 | 0.025 | 0.114 | 0.070     | 0.051         | 0.114      | 0.025      | 0.089   |
| 0.075                                      | 14  | 0.031 | 0.117 | 0.031 | 0.117 | 0.074     | 0.050         | 0.117      | 0.031      | 0.086   |
| 0.075                                      | 16  | 0.039 | 0.121 | 0.039 | 0.121 | 0.080     | 0.048         | 0.121      | 0.039      | 0.082   |
| 0.075                                      | 18  | 0.051 | 0.128 | 0.051 | 0.128 | 0.090     | 0.045         | 0.128      | 0.051      | 0.077   |
| 0.075                                      | 20  | 0.067 | 0.138 | 0.067 | 0.138 | 0.103     | 0.041         | 0.138      | 0.067      | 0.071   |
| 0.075                                      | 22  | 0.089 | 0.153 | 0.089 | 0.153 | 0.121     | 0.037         | 0.153      | 0.089      | 0.064   |
| 0.15                                       | 12  | 0.026 | 0.208 | 0.026 | 0.208 | 0.117     | 0.105         | 0.208      | 0.026      | 0.182   |
| 0.15                                       | 14  | 0.031 | 0.211 | 0.031 | 0.211 | 0.121     | 0.104         | 0.211      | 0.031      | 0.179   |
| 0.15                                       | 16  | 0.040 | 0.216 | 0.040 | 0.216 | 0.128     | 0.101         | 0.216      | 0.040      | 0.175   |
| 0.15                                       | 18  | 0.054 | 0.223 | 0.054 | 0.223 | 0.139     | 0.098         | 0.223      | 0.054      | 0.169   |
| 0.15                                       | 20  | 0.074 | 0.234 | 0.074 | 0.234 | 0.154     | 0.093         | 0.234      | 0.074      | 0.160   |
| 0.15                                       | 22  | 0.102 | 0.251 | 0.102 | 0.251 | 0.176     | 0.086         | 0.251      | 0.102      | 0.149   |

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Version 1.3, 3 November 2008

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